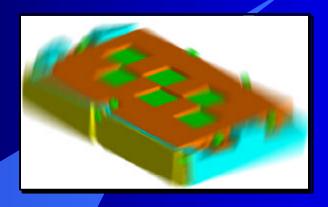
#### **FEMCI Conference**

A Multi-Disciplinary Approach to Calculate Displacement Due to Random Vibration For A Space Based Focal Plane



Anthony J. Davenport Senior Mechanical Engineer Northrop Grumman, ESSS

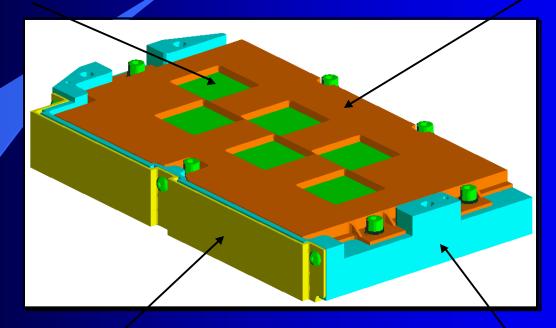




## **Focal Plane Geometry**

Filter (x6)

Cover



Flex Cable Strain Relief

**Housing** 





### So What Is The Problem?

- 1. Out of Plane Bowing from Cryogenic Loading
- 2. Random Vibration Displacement of the Cover
- 3. Lack of Material Properties (Adhesives)

Cover Filter

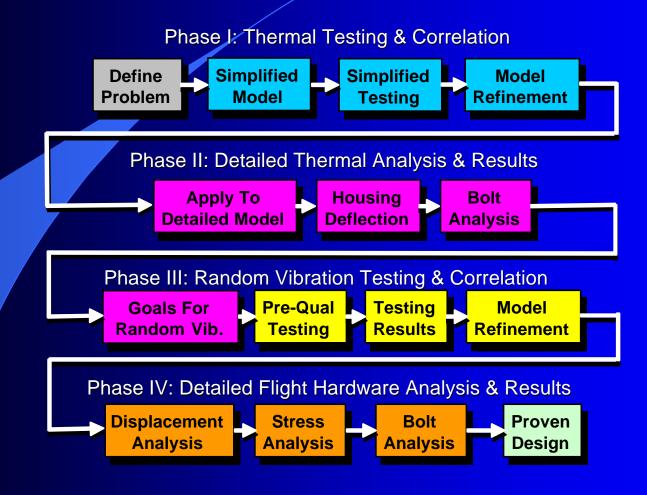
Housing Gap of Sensors
Concern

**Focal Plane Cross-Section** 





# Design & Analysis Path for the Focal Plane







### Thermal Expansion Analysis Method

- Create a simplified model in PTC's Mechanica using mechanical properties determined by the NG materials group.
  - Run model between 295 °K to 110 °K (DT = 185 °K)
  - Examine relative displacement in the out-of-plane direction (Z)
- Compare results to testing completed in laboratory and correlate model.
- Apply what is learned to detailed model.

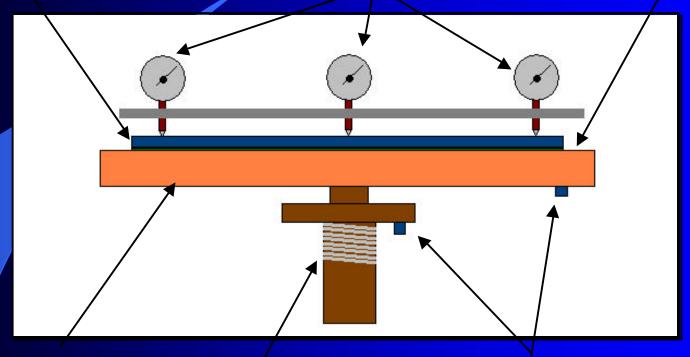




## Simplified Test Model

Substrate Dial Gages (x3)

**Adhesive** 



Molybdenum

**Cold Finger With Heater Element** 

Temperature Sensors





## **Laboratory Test Setup**



Three Dial Gages Touch
The Focal Plane in
3 Locations to Measure
Bowing in Focal Plane

Temperature Range 295 °K - 110 °K

**Measuring Dials (x3)** 

**Cold Finger & Heater** 

**Focal Plane** 



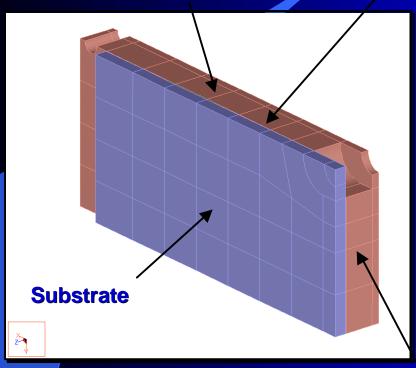


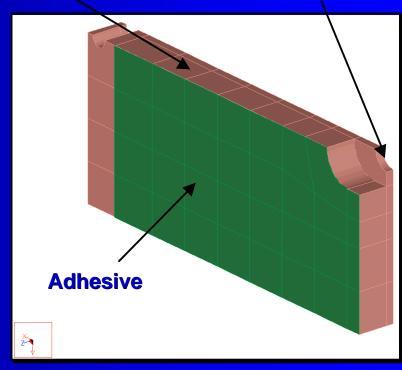
# <sup>1</sup>/<sub>4</sub> Simplified Analysis Model

Symmetry Constraint, Y

Molybdenum

Constraint, Z on Bottom Curve





**Substrate** 

Symmetry Constraint, X

Substrate Removed





# Relative Displacement Results From Testing & Analysis

**Analysis Model** 

		Displacement		
	Thickness	Trial #1	Trial #2	Average
<b>Adhesive</b>	[mil]	[mil	[mil]	[mil]
Α	5 +/- 0.1	-1.688	-1.413	-1.551
В	8 +/- 0.1	-0.775	-0.878	-0.827

**Testing** 

		Displacement		
	Thickness	Minimum	Maximum	Relative
Adhesive	[mil]	[mil]	[mil]	[mil]
Α	5 +/- 0.1	-1.979	-0.424	-1.555
В	8 +/- 0.1	-2.895	-2.046	-0.849

Comparison

		Displacement		
	Thickness	Testing	Analysis	
Adhesive	[mil]	[mil]	[mil]	% Difference
Α	5 +/- 0.1	-1.551	-1.555	-0.29%
В	8 +/- 0.1	-0.827	-0.849	-2.72%



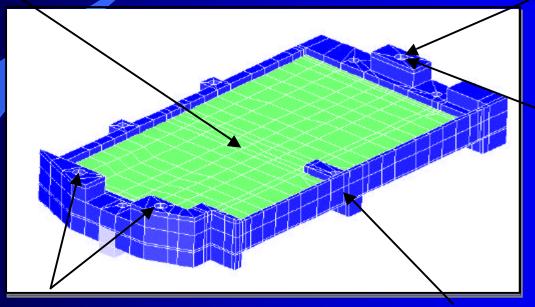


## **Detailed Analysis Model**

Focal Plane Bows 5.3 mm, or +/- 2.6 mm Across a Mid-Plane

**Ceramic Substrate** 

**Mounting Surface Z Constraint** 



X,Y Constraint

Mounting Surface Z Constraint

Molybdenum

Uniform Temperature Load: Cure to Cryogenic (295 °K to 110 °K)

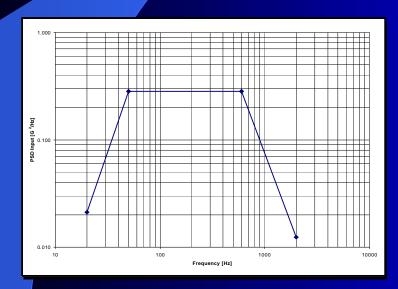




#### **Random Vibration Derived Requirements**

From Cryogenic Analysis

		Value
	Source	[in]
	Allowable (To Reduce Stray Light)	0.005
	R <sub>ss</sub> 'd Value of SCA Stack-Up	-0.00225
•	Cryogenic Bowing	-0.0002
	Outer vs. Inner SCA Tolerance	-0.0005
	Allowable for Random Vibration Deflection	0.00205

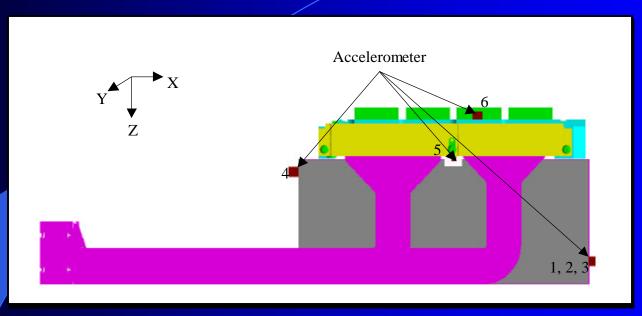


Frequency	PSD Input	
[Hz]	[G <sup>2</sup> /Hz]	
20	0.021	
50	0.282	
600	0.282	
2000	0.012	
Overall (G <sub>rms</sub> )	15.75	





## **Random Vibration Test Setup**



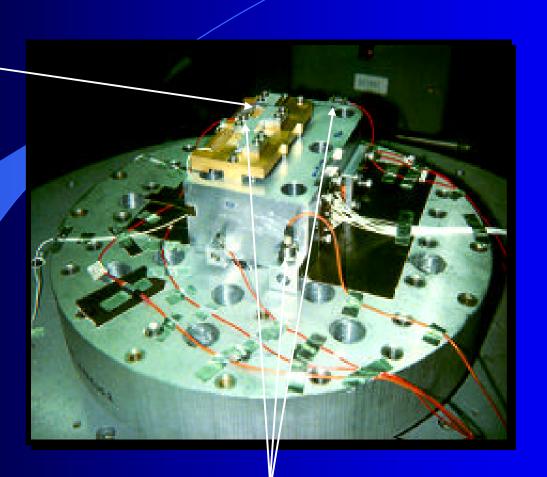
Accelerometer	Direction	Description
1	Χ	Control for X
2	Υ	Control for Y
3	Z	Control for Z
4	Z	Control for Z
5	Z	Focal Plane Cover
6	Z	Focal Plane Housing





# Test Setup

Focal Plane

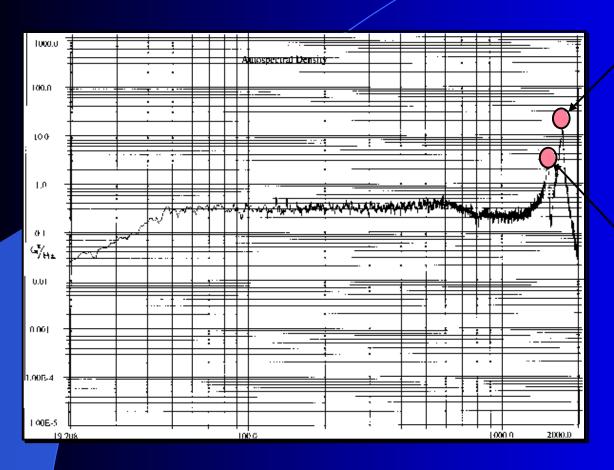


**Accelerometers** 





# Test Results: Housing



**Mode 2: 1717 Hz** 

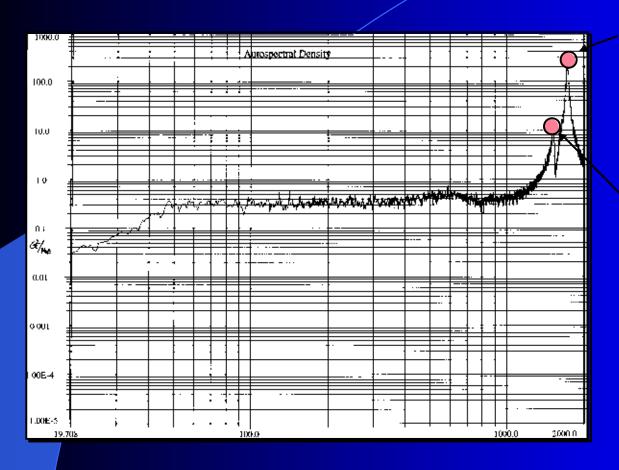
Mode 1: 1513 Hz

39.3 G<sub>rms</sub>





## **Testing Results: Cover**



Mode 2: 1717 Hz

Mode 1: 1513 Hz

118.9 G<sub>rms</sub>



#### What Can Be Derived From Test?

#### **Damping Factors**

Mode	Frequency [Hz]	PSD <sub>in</sub> [G <sup>2</sup> /Hz]	PSD <sub>out</sub> [G <sup>2</sup> /Hz]	Amplification Factor	Damping Factor
1	1513	0.019	10.55	23.6	0.02122
2	1717	0.016	193.2	109.9	0.00455

#### **3s Absolute Displacement**

	Displacement	
Channel	[mil]	Description
5	1.536	Cover
6	0.912	Housing
Sum	2.448	

Relative Displacement (500 Hz - 2000 Hz): 2.379 +/- mil Using Method Discussed in Appendix B (3% Diff.)





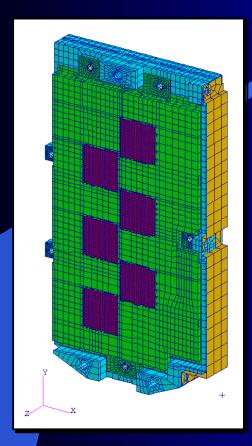
## **Method of Correlation**

- Match the Frequency of the Test Model
  - Boundary Conditions
  - Mass of Components
  - Stiffness
    - Geometry
    - Material Properties
- Match the Displacement
  - Acceleration PSD Input
  - Damping Value: z = 1/(2Q)





## **Matching Frequency**

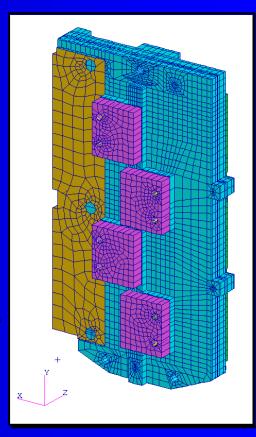


Geometry: Built from Unigraphics Model

**Boundary Conditions: Bolt Stiffness Applied** 

Mass from Tested Components

Materials: Varied Young's Modulus for Molybdenum within range found in multiple sources.

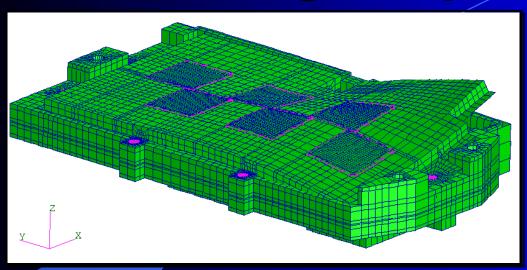


**Aniso - View** 

Iso - View

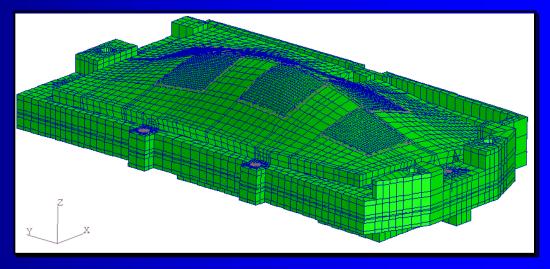


# Matching Frequency Results



Mode 1: 1477 Hz (2.4% Diff)

Mode 1: 1717 Hz (0.0% Diff)







## **Matching Displacement**

- Adjust PSD Input to Match Testing.
  - Tolerance allowed for a +1 dB overall variance.
  - For a small response, this makes a large difference.
  - It was found that the PSD input was +0.4 dB higher than Specification.
- Adjust Damping to fine tune the model (z = 0.00351)
- 2.380 mil Deflection (0.042 % diff. from testing) for 500 - 2000 Hz.





#### Conclusions

- Bowing due to Thermal Expansion is determined by defining material properties via testing, modeling, and correlation.
- Cryogenic deflections help drive the random vibration allowable.
- Random vibration correlation helps in examining future changes to the focal plane design and it's inputs.



